## 2-D $\mathbb{L} L \mathbb{R}$ YSTIALLS <br> 

HANDS-ON


In the following you will find a list of the IMAGIC commands to analyse 2D crystals in IMAGIC-5.

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Please note that there are many other commands that you probably can use during your analysis. Do not hesitate to "go your own way".

Title page:
Negatively stained 2-D crystal of bacterial D-Ribulose-1,5-Bisphosphate Carboxylase / Oxygenase (RuBisCO) after band-pass filtering (with friendly permission of Dr. Andreas Holzenburg, University of Leeds, UK)

Don't hesitate to punch "?" to understand the meaning of a certain IMAGIC-5 question). IMAGIC-5 will give you help.
(1) STARIING THE IMAGIC-5 S $\mathcal{Y S} \mathcal{T} \mathcal{M}$

Call IMAGIC:
imagic
or

## i

(or any other command name you have defined in your .cshrc or in your login.com).

## (2a) SCAN MICRO GRAPHS \& CREATE I MAGIC I MAGES

Scan the desired electron micrographs with your scanner and copy them to your workstation (see corresponding manuals).

Ulse IMAGIC command IMPORT-EXPORT to convert the images into IMAGIC format. Let us assume that the scanned micrograph is stored in $\mathcal{T} I \mathcal{F F}$ format in the file "my_crystal.tif":

```
IMAGIC-COMMAND: IMPORT-EXP
** EM2EM welcomes you **
```

```
IMAGIC-COMMAND: IMPORT-EXP
** EM2EM welcomes you **
Data format of the input to be converted : TIFF
Export to which data format [?] : IMAGIC
Input = set of 2D sections of a 3D volume: NO
Import a SET of input image files [NO] : NO
Input image file [?] : my_crystal
                                    You select
Output image file (NO EXT.) [?] : my_crystal
                            You select
Pixel spacing in Angstroem (X,Y,Z)
: 5.0
You select
```

For further information on how to use the IMPORT-EXPORT command ple ase see the "em2em" manual.

## (26) $\mathcal{C H E C \mathcal { T } \mathcal { H E } I M A G E S}$

Ulse IMAGIC command DISPLAY to check the images.

You can also calculate a power spectrum of your crystalline image to checkits quality. Call FFT2D and use option FORWARD (see chapter (6)).

Then DISPLAY the Fourier transform. DISPLAY will automatically show you the (logaritim of the) power spectrum of the transform.

## (3) $I \mathcal{M A G E} S I Z \mathcal{E}$

One will normally extract from the larger raw image a smaller area containing the crystal of interest. To find the co-ordinates of the smaller area, we use the COOS option together with the NO STORE option in the DISPLAY command:

```
IMAGIC-COMMAND: DISP
** DISPLAY welcomes you **
Input image file, image loc#s : my_crystal
                                    you select
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,BYE...) ? [NO] : COOS
Should the values be stored in a PLT file?: NO STORAGE
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,BYE . . .) ? [NO]: NO
```

One normally needs to know the top-left $X$ - $\mathcal{Y}$ co-ordinates as well as the bottom-right co-ordinates. To find the corresponding co-ordinates move the cursor to the top left edge and press the middle button of the mouse. DISPLAY will print the co-ordinate values on the screen. Continue with the lower right edge. If you want to stop select the same point twice.

Continue which the next crystalline area or le ave DISPLAY by typing BYE or EXIT.

This way we know how large the extracted image should be and where it starts. The actual extraction is performed by the command CUT-IMAGES (option GENERAL):

```
IMAGIC-COMMAND: CUT-IM
** SUBFILE welcomes you **
Input file, image loc#s : my_crystal
Output file, image loc#s : crys_patch,1
select
Mode of operation:
    APERIODIC, CENTER, GENERAL, PAD_GENERAL,
    LARGE_PAD, SMALL_PAD, PERIODIC, SQUARE,
    CHECKERS
Give mode of operation : GENERAL
Output file dimensions X,Y : 100,100
Top left X, Y coordinates
in the old image : 23,18
```

you select according to the values found with DISPLAY/COOS

Another way to extract the crystalline area is to take the coordinates of the centre of the desired region.

These coordinates are determined with command DISPLAY (option COOS) and stored in a file (COOS option: YES STORE):

```
IMAGIC-COMMAND: DISP
** DISPLAY welcomes you **
Input image file, image loc#s : my_crystal
                                    you select
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,SAVE,BYE . . ) ? : COOS
Should the values be stored in a PLT file? : YES
Output PLT file [my_crystal] : my_crystal
Change parameter settings
(ERASE, SCALE, LOC, START, SCAN, SAVE, BYE. ..)? : NO
```

In the example the centralcoordinates are stored in file my_crystal.plt.

You can again use command CUT-IMAGE, now with option APERIODIC to extract the desired crystalline patch(es):

```
IMAGIC-COMMAND: CUT-IM
** SUBFILE welcomes you **
Input file, image loc#s : my_crystal
Output file, image loc#s : crys_patch,1
you
select
Mode of operation:
    APERIODIC, CENTER, GENERAL, PAD_GENERAL,
    LARGE_PAD, SMALL_PAD, PERIODIC, SQUARE,
    CHECKERS
Give mode of operation : APERIODIC
Output file dimensions X,Y : 100,100

\section*{\(\mathcal{N O T E}:\)}

The image dimensions should be chosen such that they are compatible with the \(\mathcal{F F}\) (T algorithm (preferably factors of 2,3 and 5). To find out interactively which sizes are compatible, type a ? when the CUT-IMAGES command prompts you for the image size.

Finally, make the image size square. Although this is not strictly necessary, this will facilitate your thinking. If you have a rectangular region of interest, you can impose an ellipse on the square image later on using PRETREAT-IMAGE (see later).

\section*{(4) \(\mathcal{B A N}\) - PASS FILIER}

This is an operation that can be performed at different stages of the analysis. However, it shall be introduced here since it is a form of image preparation and can be logically done here. This is an optionaloperation. Proceed to section (5) if desired.
\(\mathcal{A}\) band-pass-filter can be used to suppress the very low and the very figh spatial frequencies. The very high spatial frequencies represent noise that will affect the analysis, and so we would like to ameliorate its effects quite early on. The very low spatial frequencies represent things like average densities and density ramps that depend on illumination conditions and fave nothing to do with the molecular structure in which we are interested. For crystal analysis, all the low frequency information up to the first order reflections can be left out without affecting the information we are interested in. For correlation ave raging it even should be left out.

The (INCORE-)BAND-PASS-FILTER command Fourier transforms (FFFT) the input image and imposes a mask on it that attenuates low and high frequencies, but lets intermediate ones through. The inverse \(\mathcal{F o u r i e r}\) transform is also computed automatically. The parameters requested are the low frequency cut-off and the high frequency cut-off. These depend on the situation at hand, e.g., how much noise is present in your images and how finely they have been digitised. However, the default values are reasonable. Also, one is requested for the percentage remaining transmission of low frequency. For example, a value of 0.02 means that the low frequency Fourier components are \(\mathfrak{N O T}\) set to zero 6ut instead are multiplied by 0.02. Thus, although they are suppressed now they can be re-boosted to their original values using the command INVERSE-BAND-PASS-FILTER. You cannot retrieve the high frequency components, however.
```

IMAGIC-COMMAND: INC-BAND-PASS
** INCBAND welcomes you **
Give input file, loc\#s : crys_patch
Give output file, loc\#s : crys_filt
Inverse band-pass filter : NO
The image will be band-pass filtered
Please specify:
Low frequency cut off : 0.05 have to be adapted
Remaining low-freq. transm. : 0.005 (see text above),
High frequency cut off : 0.02 to get started the
default values can
help you
ASQ filter the images too? : NO

```

If you want to calculate your frequency cut-off in terms of spatial frequency, then here is an example. Say that the image is scanned such that each pixel is of size \(x\). Then in the \(\mathcal{F}\) ourier transform, the edge of the image corresponds to the maximum spatial frequency \(1 /(2 * x)\). Remember that the centre of the transform is zero spatial frequency. Thus a fraction \(f(6 e t w e e n 0\) and 1) corresponds to a spatialfrequency of
\[
\frac{f}{2 * x}
\]

Note:
If your images are too large (i.e., do not fit in core) please use command BAND-PASSFILTER.

\section*{(5) PREPARATION OF THE CRSS TAL I MAGE}

Prior to any analysis one will normally prepare the image so to avoid some obvious artefacts and to bring the statistical properties of the image such as average density and variance to standard values.

\section*{(5a) ISPOSE- PLI - CONTOUR}

If the crystal does not quite fill the image one may mask the surrounding background away by contouring the crystal area. The coordinates of the contour are determined with command DISPLAY using the COOS option. The mask is actually imposed later using the command IMPOSE-PLT-CONTOUR. The image statistics inside the contour are normalised meaning that the average density is set to zero and the standard deviation of the image to 10:
```

IMAGIC-COMMAND: IMPOSE-PLT
** CONTPLT welcomes you **
Input file, image loc\#s : crys_filt
Contour file name : crys_filt you
Output file, image loc\#s : crys_norm select
Normalise densities inside contour : YES

```

\section*{(56) PRETREAT - IMAGE}

If the crystal fills the larger part of the image one may standardise the statistics in the whole image or within a circular maskin the image, in which situations one uses the command PRETREAT-IMAGE.
```

IMAGIC-COMMAND: PRETREAT-IMAGE
** PRETREAT welcomes you **
Input file, image loc\#s : crys_filt
you
Output file, image loc\#s : crys norm
: crys_norm select
Mode of pretreatment:
MASKONLY NORMVARIANCE NVNOMASK ZEROFLOAT
Please specify option : NORMVAR
Pretreatment mask to be used
CIRCLE RECTANGLE : WHOLE
Give the desired new sigma : 10.0

```
\(\mathcal{N O} \mathcal{T E}:\)

In all important operations (FFFI) during the analysis, images are treated as being cyclical. It is therefore very important to avoid having the image information extend to the edge of the image. This can be avoided by using a mask (as above) or by padding an image with an edge of zeroes (IMAGIC command: CUT-IMAGES with options SMALLPAD or GENPAD).

\section*{}
\(\mathcal{N}\) Normally images are analysed in which protein (ingeneral: the density of the particles to be analysed, correlated etc.) appears light on the display, whereas negative stain, for example, appears dark. After floating and normalisation of densities above, this means that higher (positive) density values should represent protein, i.e., desired structural information. This may not be the case with your images. If not, then use the command MULTIPLY-BY-CONSTANT, option MULTIPLY to multiply your image by - 1.0 at this stage. Otherwise, just carry on.
```

IMAGIC-COMMAND: MULTIPLY-BY-CONST
** ARITHM welcomes you **
Input file, image loc\#s : crys_norm
Output file, image loc\#s : crys_norm
Choose arithmetic operation : MULT
Give CONSTANT to be multipl. to each pixel : -1.0

```
(6) THE FO URI ER TRANS FO RS AND THE TO WER S PECTRUM

For periodic objects like a \(2 \mathcal{D}\)-crystal of biologicalmacromolecules it is worth looking at the \(\mathcal{F o u r i e r ~ t r a n s f o r m ~ s i n c e ~ t h e ~ p e r i o d i c ~ i n f o r m a t i o n ~ i s ~ c o n c e n t r a t e d ~ o n ~ a ~ r e g u l a r ~}\) "reciprocal lattice". All the non-periodic information lies outside the reciprocallatice peaks and that allows us to, for example, place a maskover the transform that le ts the peaks through and stops everything else (FOURIER-PEAK-FILTERING).

The Fourier transform from the input image is calculated by using the command FFT2D with option FORWARD:
```

IMAGIC-COMMAND: FFT2D
** FFT2D welcomes you **
Input file, image loc\#s
: crys_norm You
Output file, image loc\#s : crys_fft select
Forward or Reverse Fourier transform : FORWARD

```

We can thenlook at the Fourier transformed image by using the \(\mathcal{D I S}\) PLAS command. If not otherwise specified DISPLAY will by default display the logarithm of the squares (i.e. the log the power spectrum) whenever complex (Fourier transformed) data are to be displayed. The default GREYVALUES are 0.0 and 5.0 , respectively. It may be worth playing a bit with these values to find the optimum representation of the power spectrum. For example, 1.5 to 4.0 :
```

IMAGIC-COMMAND: DISP
** DISPLAY welcomes you **
Input image file, image loc\#s : crys_fft
you select,
Fourier transform
of your crystal
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,BYE...) ? [NO] : GREY
Please give option to get the greyvalues
(AUTOMATIC,INTERACTIVE,WINDOW) [AUTO] : INTERACTIVE
Give black, white levels (0,0 = automatic): 1.5,4
\bullet••
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,BYE . . ) ? [NO] : NO

```

\section*{\(\mathcal{N} O \mathcal{T E}:\)}

The Fourier transform is always transposed ( \(X-\mathcal{Y}\) exchanged) as compared to the input image. For publications, etc., the transposing can be undone by using the command TRANSPOSE-IMAGE.

\section*{(7) \(\mathcal{D E T E R M I N I N G ~ T H E ~ R E C I P R O C A L ~ L A T I I C E ~ V E C T O R S ~}\)}

The first step is to get an approximate idea about the positions of the diffraction peaks. For this purpose we DISPLAY the Fourier transformed image and then use the COOS option (reads the cursor position in terms of the image coordinates) to position reciprocallattice peaks.
```

IMAGIC-COMMAND: DISP
** DISPLAY welcomes you **
Input file name, image loc\#s
: crys_fft
Fourier transform
of your crystal
Change parameter settings
(ERASE,SCALE, LOC,START,SCAN,BYE...) ? [NO] : COOS
Should the values be stored in a PLT file?: NO
Change parameter settings
(ERASE, SCALE, LOC, START, SCAN, SAVE, BYE . . .) ? [NO] : NO

```

You have to index the diffraction pattern, that is, to determine what the unit cell is. See fandbooks on diffraction methods and lookfor the 17 possible plane patterns.

Then we use the command FOURIER-PEAK-SEARCH to get the precise positions of the diffraction peaks. In this command, a least- squares fit is performed on a \(3 \times 3\) environment of the peak to find refined peakcoordinates. \(\mathcal{A}\) list of the peaks is stored in a "plt" file which you should send to a printer.
```

IMAGIC-COMMAND: FOURIER-P-S
** ALLPEAK welcomes you **
Input file, image loc\#s : crys_fft
you select,
Fourier transform
of your crystal
Output filename for peak coordinates : crys_peaks.plt
you select,
output "plt" file
with coordinates
Linear size of search area (3-5-7-9-11) : 5 you select
Minimal distance allowed between peaks : 100 youselect,
unit cell is
minimum
you select,
1/2 unit cell
is minimum
Mode of operation
NORMAL, DEVIATION : normal
Number of peaks wanted maximally
: 300
depends on your
crystal, be conservative
at the beginning

```

Instead of using option NORMAL you may prefer option DEVIATION in which peaks are only selected if the peakheight is higher than a specified standard deviation added to the background (type ? to get he (p).

Lookfor the peaks that fall on the lattice and calculate the refined reciprocallatice coordinates from these refined peak positions. Note: because of the Hermitian symmetry the diffraction peaks come in pairs (Friedel pairs).

Youcanthencheck the positions of the peaks with command DISPLAY and option PLOT.

Finally, use the command COMPUTE-RECIPROCAL-VECTORS to convert the peak coordinates from the peak list into true reciprocal lattice vectors. Really, though, you only just need a pocket calculator.

\section*{}

Uling the command FOURIER-PEAK-FILTER we can focus on the periodic information present in the image and disregard everything else. If the crystal is large and ideally well ordered, the peaks in the Fourier transforms would be only one pixel wide and would have a perfectly defined phase. However, in practice things look different; peaks may be smeared out over an area and we thus are obliged to use foles containing more than a single pixel in Fourier space.

The fole size parameter is a very important one. It determines the effective area over which one averages in real-space. The smaller the hole, the more unit cells are averaged into each point of the resulting filtered image. The (line ar) size of the averaged area in real-space may be roughly estimated by the formula:
\[
\text { Linear Averaging Size }=\frac{\text { Linear Image Size }}{2 * \text { Hole Radius }}
\]
\(\mathcal{N O T E}: \mathcal{T h}\) is FOURIER-PEAK-FILTER command does only the masking. You thus must provide it with an input Fourier transform (command FFT2D, option FORWARD), and you will have to reverse Fourier transform (command FFT2D, option REVERSE) the masked transform to obtain an image you can lookat.
```

IMAGIC-COMMAND: FOURIER-P-FILT
** FOUFILT welcomes you **
Input file, image loc\#s ? : crys_fft
you select,
Fourier transform
of your crystal
Output file, loc\#s?
: crys_opt_filt
you select
Mode to get the mask characteristics.
Input from USER or FILE : USER
Reciprocal lattice vector 1 : X1 , Y1 : 12.3,11.6 you
Reciprocal lattice vector 2 : X2 , Y2 : 8.2,6.3 have
to know
Give radius of HOLES in mask (pixels) [2]: 4 you select
Low pass filter radius [0.667] : 0.8 you select
Leave out the (0,0) peak [YES] : YES you select,
usually: YES

```

During the masking of the Fourier transform, the program will determine in detail fow coherent the phases in each hole of the masked image are. A quality factor \(Q\) is calculated which is defined to be:
\[
Q=\frac{\text { Vector Sum of Peak Amplitudes }}{\text { Sum of Moduli of Peak Amplitudes }}
\]

A significance threshold for \(Q\) is also defined and printed. Note that, unless the crystal is ideal and centred, it may be very difficult to interpret the peak phases directly in terms of the plane group of the crystal.
\(\mathcal{N O T E : ~ T h i s ~ K i n d ~ o f ~ p r o c e s s i n g ~ ( F O U R I E R - P E A K - F I L T E R ) ~ i s ~ n o t ~ v e r y ~ s u b t l e ~ s i n c e ~ i t ~ i s ~}\) based on the implicit assumption that the input crystal is a perfect crystal with a repeating motif placed on an ide al undistorted lattice. CORRELATIONAVERAGING is much more subtle and can replace/ supersede this Fourier space manipulation procedure almost always see chapter 10).

\section*{(9) THE "QUAS I OPI I CALLY" FI LIERED I MAGE}

The filtered image has some interesting interpretations. In each point this image contains the local average of an environment of the input (unfiltered) image. Thus, if the foles are not chosen too small, the filtered image will still contain all the long range distortions present in the original and can thus be used as a first judgement of quality.
\(\mathcal{A l s}\), , 6 ad areas of the crystal may be recognised visually in the filtered image.

Yet, quasi-optical filtering does not allow us to correct for the distortions and thus the possibilities are fundamentally limited. The number of unit cells averaged is limited to the characteristic "coherency" area of the crystal.

\section*{(10) \(\operatorname{CORRELATIO\mathcal {AVERAGING}\text {AV}}\)}

Correlation averaging (CA) allows us to correct for long range distortions of the crystal and thus allows us to average a much larger number of unit cells than with the filtering technique.

To apply correlation averaging we need a reference image since we are essentially looking for "matches" of the reference motif ("matched filtering") in the crystalimage. The choice of the reference is important and some attention must be devoted to create good reference images.

\section*{(10a) LOOX FOR A REFERENCE IMAGE}

\section*{(i) Extracting a patch from the filtered image}

Since the quasi-optically filtered image already contains considerably less noise than the original it is a good idea to extract an area from that image to be used as a reference patch for the correlation image.

The extraction can be done in the following way: DISPLAY your quasi-optically filtered image. If the image is displayed use option COOS. Move the cursor to the middle of a good area and press the middle button of the mouse. You are asked whether the coordinates should be stored, give YES and specify the name of the output ".plt" file (usually the same name as the input file). To stop press the middle button and give STOP. Leave DISPLAY by typing BYE or EXIT.

To extract the small reference patch use command CUT-IMAGE with option APERIODIC. Input file is the quasi-optically filtered image and the corresponding "plt" file created in IMAGIC:
```

IMAGIC-COMMAND: CUT-IM
** SUBFILE welcomes you **
Input file, image loc\#s
Output file, image loc\#s
: crys_opt_filt
you
: crys_ref
Mode of operation:
APERIODIC, CENTER, GENERAL, PAD_GENERAL,
LARGE_PAD, SMALL_PAD, PERIODIC, SQUARE,
CHECKERS
Give mode of operation : APERIODIC
Output file dimensions X,Y : 100,100 you select,
type ? to
get "good" image
sizes. The value
depends on the
size of the unit
cell of the crystal
Coordinates (plt) file : my_micrograph.plt
output from
DISPLAY
(option COOS)

```
(ii) Using a patch from the original image as reference

We can also start with a patch of the original crystal as a reference. For that purpose we simply extract a good sub-area of the full crystal instead of using the quasioptically filtered image. The same commands shown in (i) can be used.

\section*{(106) \(\mathcal{E N} \mathcal{N} \operatorname{RI} \mathcal{N} G \mathcal{T} \mathcal{H} \mathcal{E}\) " \(\mathcal{M O} \mathcal{T} I \mathcal{F}^{\prime}\)}

Once we have selected a reference patch we should try to centre the motif in the (still small) reference image. Call command CENTER-IMAGE and use options SELF or MASS. Type ? to get he(p):
```

IMAGIC-COMMAND: CENTER-IM
** ALIMASS welcomes you **
Input file, loc. numbers : crys_ref you
Output file, loc. numbers : crys_ref_cent select
Options for centering:
MASS MASK ABSOLUTE SELF CENTER
Please specify option : mass type ? to
get help
Radius of circle for mass calcn : 0.85
you
Density threshold for mass calcn : -999.
select,
-999. means
no threshold

```

If the first reference is a patch from the original noisy crystal, it may be difficult to centre this noisy reference and one may wait until after the first iteration(s) of the correlation averaging procedure with the centring of the reference image. If the reference image is not centred, that leads to correlation peaks which will be systematically shifted with respect to the unit cell of the crystal. This may become a problem if the reference patch is of the same order of size as the unit cell. In this case the reference image size should be larger than the unit cell.

\section*{(10c) PADDING WITH ZEROES}

For the cross-correlation function calculation, the image and reference image fave to be of exactly the same size. For this reason the small reference image fas to be padded with zeroes up to the size of the crystalimage.

To achieve this, use command PAD-IMAGE with option CENTER.
```

IMAGIC-COMMAND: PAD-IM
** SUBFILE welcomes you **
Input file, image loc\#s : crys_ref_cent
Output file, image loc\#s : crys_ref_ca
Mode of operation:
APERIODIC, CENTER, GENERAL, PAD_GENERAL,
LARGE_PAD, SMALL_PAD, PERIODIC, SQUARE,
CHECKERS
Give mode of operation : CENTER
Output file dimensions X,Y : 1024,1024 size of the
crystal image

```

\section*{(10d) CROSS-CORRELATION}

To start the correlation averaging procedure you must start the CORRELATIONAVERAGING command. This command will perform all the operations mentione d below up to the levelof iterating the whole procedure (chapters (10e) and (11)).

The cross correlation function (CCF) or the mutual correlation function ( \(\mathcal{M C F}\) ) is calculated by (conjugate) multiplying the Fourier transforms of the crystal image and the reference image with each other. The result is then Fourier transformed back to real space and is the \(\mathcal{C C F}\) (or \(\mathcal{M C F}\) ) image containing a peak at each position where the original matches the reference.

The correlation peak heights are determined by how well an area of the crystal matches the reference motif. However, factors such as the local amount of embedding material (stain) in a given area or other lowfrequency disturbances which are not (necessarily) structure related may lead to misleading correlation peak values. It is therefore a good practice to suppress the low frequency components during the CCF calculation. This can be done by either BAND-PASS-FILTERing the crystal input image (see chapter (4) or by multiply the CCF in Fourier space by a filtering function (command ARITHMETIC and option BANDPASS).

The peaks in the CCF (or \(\mathcal{M C F}\) ) are searched and written into a (sorted) table of the so-many highest peaks that were found in the CCF. The peak searching algorithm performs a least-squares-fit of a paraboloid over a \(3 \times 3\) environment of the peaks and thus finds peaks coordinates within a fraction of the inter pixel distance. The algoritfin is the same as that mentioned earlier to find the peaks within the power spectrum of the crystalimage.

\section*{(10e) EXTRACTING THE S MALL PATCHES}

Using the \(\mathcal{C C F}\) (or \(\mathcal{M C F}\) ) peak list, CORRELATION-AVERAGING then extracts the environments of the correlation maxima from the input crystalimage and puts these as a sequence of small images in a standard IMAGIC image file. Ple ase note that (at the moment) the sub-images are only extracted at integer co-ordinate positions.

The whole correlation averaging procedure is calculated with IMAGIC command CORRELATION-AVERAGING:
```

IMAGIC-COMMAND : co-aver
** COR_AVG welcomes you **
Input crystal (patches) : crys_norm
your crystal
FULL analysis or NEW peaks only : FULL
Input REFERENCE patch
Mode of operation
CCF or MCF : CCF
at the beginning
we prefer CCF
Give name for CCF file [crysccfs] : crys_ccf
output CCF file,
you select

# of PEAKS exp. in data set : 500

                    be conservative at the
                    beginning. Check the
                                    extracted patches later
                                    to correct this number
                                    in further iteration(s)
    Distance from the edge of file [32] : 50
Minimal distance between peaks [10.] : 100
you
select,
depends on
the size of the
reference motif
Name for extracted patches
Size of these subfiles [64,64]
. Junk_ref_ft
2nd scratch file needed : junk_xxx select

```

\section*{(10f) S UMMING THE S MALL PATCHES}

Then all the images are summed into a total sum which can be inspected and may be used to re-iterate the process. Ulse command INCORE-SUM with option TOTSUM:
```

IMAGIC-COMMAND: INC-SUM
** SUMMER welcomes you **
Mode of summing:
CONDITIONAL_SUM, SOME_SUM, TOTAL_SUM
Please specify option : TOTSUM
Input file, NO loc\#s : crys_sml
you select
Output file, image loc\#s : crys_sum output from
Standard deviation images : none

```
\(\mathcal{N}\) ote that since the peak-list is sorted by correlation values, the first of the extracted patches may be better than the last ones. It may thus be wise to restrict the analysis to the first so-and-so-many extracted images.

If desired, you can use the INCORE-SUM command with the SOMESUM option to sum only the first 100 or so of your extracted images, and not all of them.

\section*{(11) I TERATI NG THE CORRELATI O N AVERAGING PRO CEDURE}

Each time correlation averaging procedure is repeated, a better average is obtained with less noise. Since it has less noise, we may make the reference patch smaller and that, in turn, leads to a better correction of the distortions of the crystal.

Do not forget, fowever, to centre the motif since with a small, uncentred reference patch you may miss the molecules in the CCF.

In a later stage of the analysis the finer details will become more and more important. \(\mathfrak{M C F}\) can then be used inste ad of \(\mathcal{C C F}\).

\section*{(12) \(\mathcal{M S}\) CLASS I FICATIO \(\mathcal{N}\) O \(\mathcal{T H} \mathcal{E X}\) ERACTED PATCHES}

The analysis up to this point has considered that the crystal might have been distorted but we have always assumed that the unit cells are equal. This may \(\mathcal{N O T}\) be true. Differences in preparation, rotational shifts of the molecules within the unit cell, small molecular differences etc. cannot be detected with the procedure which we have used untilnow.

To find differences between the patches we first use multivariate statistical analysis ( \(M S \mathcal{A}\) ) (representation of the extracted patches in a "hyper space" and data reduction) and automatic classification.
(12a) MS A MAS K

First a MSA maskis needed which is a binary mask to define the are a of interest within the image frame that should be considered during multivariate statistical analys is and classification.

For this, DISPLAY the resulting average image of the previous correlation ave raging procedure (use a large SCALE factor). Then use options COOS and YES OUTPUT TO PLT FILE (store), and mark the boundary (not very close) around the interesting area.

Having created this contour "plt" file, call MSA-MASK:
```

IMAGIC-COMMAND: MSA-MASK
** MSAMASK welcomes you **
Input file, image loc\#s : crys_sum
you select,
average of the
extracted patches
Input contour coos (plt) file [cry_sum] : totsum_X.plt
contour "plt"
file created
with DISPLAY
and option COOS
Give output file, image loc\#s : msamask
you select

```

\section*{(126) MULIIVARIATESTATISTICAL ANALYSIS (MSA)}

Then perform multivariate statistical analysis. Input images are the patches extracted from the previous correlation procedure. The results are mainly stored in the fieader file of the input images, in a registration file (msa.lis, for example) and in the (output) eigenimages (eigenim, for example).

Call MSA-RUN:
```

IMAGIC-COMMAND: MSA-RUN
** MSA welcomes you **
Choose mode of operation:
FRESH_MSA REFINE
Please specify option : fresh
MSA distances:
EUCLIDIAN CHISQUARE MODULATION
Please specify option : modulation
use modulation distance
: crys_sml
you
select,
extracted patches of
correlation averaging
: no
if wanted some patches
can be excluded
: msamask
the MSA mask created,
you can give "none"
if no mask is wanted
Eigenimages output file
Pixel coordinates output file
: eigenim output
: pixcoos you
Eigenpixel vectors output file
Give number of iterations (<65) [24] : 24 you select
: eigenpix select
Give number of eigenimages (<70) [24] : 69 you select
Overcorrection factor (0< ocf< 0.9) : 0.8 you select
Rootname for results files, no ext. : msa you select
no extension please!

```

\section*{(12c) CLASSIFICATION}

The next step is the classification within the hyper-space created by MSA-RUN. Call MSA-CLASSIFY:
```

IMAGIC-COMMAND: MSA-CLASSIFY
** CLASSIFY welcomes you **
Input to be classified:
IMAGES PIXEL-VECTORS SEQUENCES FABOSA-CONTOURS
Please specify option : images
Input images file (treated by MSA) : crys_sml
extracted crystal patches
treated by MSARUN
Percentage of images to be ignored [0] : 0
Active factors for classification? [68] : 68

```

\section*{the number must be less/equal the one used in MSARUN}
```

Tricky normalisation of factorial coos : no always NO!

```
Tricky normalisation of factorial coos : no always NO!
Weight the factorial coordinates [NO] : no always NO!
Weight the factorial coordinates [NO] : no always NO!
Plot the classification trees [YES] : no usually NO!
Plot the classification trees [YES] : no usually NO!
Other than default output information : no
Other than default output information : no
Classification (MSA) maps stored [NO] : no
Classification (MSA) maps stored [NO] : no
What NUMBER of classes do you wish : 500 you select!
What NUMBER of classes do you wish : 500 you select!
                                    large number
                                    large number
Name of output results files : classes
Name of output results files : classes
    you select!
    you select!
Mass threshold parameter [0]
Mass threshold parameter [0]
    0
```

    0
    ```

MSA-CLASSIFY asks for the number of classes into which the data set should be divided. Try to start with a fuge number, use MSA-SUM (12d) and look how the class. sum images look like. If too many classes show the same view you can reduce the number of classes (call MSA-CLASSIFY (12c) and MSA-SUM (12d). MSA-RUN (12b) is not necessary).

\section*{(12d) CLASS - S UM IMAGES}

Then calculate the class-sum images. Call MSA-SUM-IMAGES:
```

IMAGIC-COMMAND: MSA-SUM
** CLASSUM welcomes you **
Input images to be summed : crys_sml
extracted crystal patches
treated by MSA and CLASSIFY
Rootname of input classification files : classes
output from MSACLASSIFY
Output class averages [classums]
: classums
you select, output patch averages
Downweight small classes? [YES] : yes
Produce summing statistics
: no
Fraction of worst class members to ignore: 5 you select

```
\(\mathcal{N}\) ow look at the class-sum images, if necessary re-do the classification (steps \(12 c\). 12d) demanding less or more number of classes.

\section*{(13) PUBLICATION}

Commands which you may need for polishing your results are, for example: BLOW-UP to bring up the image to a larger format (by interpolation), CONTOUR-IMAGE to create contour lines (but be careful not to interpret too many contour lines and hence less "objectivity"), AVERAGE-NFOLD-ROTATIONAL to impose in-plane symmetries, INFORMATION-IN-SEQUENCE to calculate various resolution crite ria... See manual(s) to get information about all available IMAAGIC commands or use command MENU * .

Then write a nice paper for \(\mathfrak{N a t u r e}\), \(\operatorname{Science,~Structure,~} \mathfrak{g} \mathfrak{M B}\), etc. Or youmay feelthat the most appropriate thing to do at this point is command DELETE-IMAGE and go have a beer (the latter option is not yet implemented in IMAGIC).

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